Does transferring my domain incur any downtime for my website?

No, the transfer process will in no way affect the functionality of your website or email.

https://support.lexiconn.com/kb/questions/107/